

STATISTICS

WORKSHEET-1

I. Explain MEDIAN, MODE, MEAN

To find the median, mode and mean of the following values:

3,1,4,6,12,9,4

Step 1: Arrange the values in ascending order

1,3,4,4,6,9,12

Step 2: Find the value of the middle term

1,3,4, **4**, 6,9,12

4 is the median

Step 3: The value, which occurs most of the time, is the mode.

1,3,**4**, **4**, 6,9,12

4 occurs maximum number of time, which is twice in this case. Therefore 4 is the mode

Step 4: Now add all the values.

$$1+3+4+4+6+9+12=39$$

$$\text{Therefore Mean} = \frac{39}{\text{number of the values}}$$

$$\text{Total number of the values} = 7$$

$$\text{Mean} = \frac{39}{7} = 5.57$$

Questions:

1. Find the median.

8,9,10,6,7

2. Find the median.

8,11,9,5,7

3. Find the mode of the following numbers

3,7,9,8,3

4. Find the mean.

2,5,6,8,4

5. Find the median, mean

1,5,12,10,12,2,3

6. Find the median, mode and mean

1,4,5,12,15,12,10,10,12

7. Find the median.

(TBSE-2008)

8,9,10,6,7,8,10,6,9,5,7

8. Find the mode of the following numbers

4,2,5,4,2,7,4,3,6,3,4

(TBSE-2009)

9. Write the median of 9, 4, 12, 7, 2

(TBSE-2011)

10. Find the median of the following numbers

5,6,3,7,4,9,6,4,8,3,5

(TBSE-2014)

WORKSHEET-2

II. Explain **median** for **even** number of terms.

e.g. the following values are given 3,1,4,8,6,11,9,12

Step1: Arrange the values in ascending order

1,3,4,6,8,9,11,12

Step2: Find the middle value

1,3,4, 6,8, 9,11,12

As there are two middle values. Median would be the average of **6 & 8**

$$\text{Median} = \frac{6 + 8}{2} = 7$$

Questions:

1. Find the median of the following numbers
5,2,9,8,4,12
2. Find the median of the following numbers
12,7,15,12,10,8,3,4

III. To find the missing value when mean is given.

e.g. Find the value of x when the mean of the following numbers 1,2,4,5,x and 7 is 4.

$$\text{Mean } (\bar{x}) = \frac{1+2+4+5+x+7}{6}$$

$$\Rightarrow 4 = \frac{19+x}{6}$$

$$\Rightarrow 24 = 19 + x$$

$$\Rightarrow 24 - 19 = x$$

$$\Rightarrow x = 5$$

Questions:

1. If the arithmetic mean of 1,2,5,6,x & 8 is 5. Find the value of x.
2. If the arithmetic mean of 4,8,3,x & 11 is 7. Find the value of x.
3. If the arithmetic mean of 6,4,7, p & 8 is 5. Find the value of p.
4. If the arithmetic mean of 6,8,9, p & 13 is 10. Find the value of p.
5. If the arithmetic mean of 3,6,8,4, x & 2 is 4. Find the value of x.

WORKSHEET-3

IV. If the arithmetic mean of 1,2,4,5,5 & 7 is 4. Find the value of $(1-4)+(2-4)+(5-4)+(5-4)+(7-4)$.

If the arithmetic mean of 3,4,8,9 & 11 is 7. Find the value of $(3-7)+(4-7)+(8-7)+(9-7)+(11-7)$.

Questions:

1. If the arithmetic mean of $x_1, x_2, x_3, \dots, x_n$ is \bar{x} . Find the value of $(x_1 - \bar{x}) + (x_2 - \bar{x}) + (x_3 - \bar{x}) + \dots + (x_n - \bar{x})$
2. The arithmetic mean of $x_1, x_2, x_3, \dots, x_n$ is \bar{x} . If a is added to each of these numbers. What will be the mean of the new numbers?

V. **Empirical formula.**

$$\text{Mode} = 3\text{Median} - 2\text{Mean}$$

Question:

1. The arithmetic mean and median of a frequency distribution are 42.3 and 41.9 respectively. From the empirical relation of AM, median, mode, find the mode.
2. The arithmetic mean and median of a frequency distribution are 8 and 7.8 respectively. Find the mode.
3. The mode and median of a frequency distribution are 10 and 10.5 respectively. Find the arithmetic mean
4. The arithmetic mean and mode of a frequency distribution are 6 and 6.1 respectively. Find the median.
5. The arithmetic mean and mode of a frequency distribution are 42.3 and 41.1 respectively. Find the median.

WORKSHEET-4

VI. Grouped data.

i) Arithmetic mean of grouped data.

Find the arithmetic mean of the following data.

| | | | | | |
|----------------|------|--------|---------|---------|---------|
| Class interval | 0-50 | 50-100 | 100-150 | 150-200 | 200-250 |
| Frequency | 15 | 20 | 35 | 20 | 10 |

Solution:

| Class interval | Mid point(x) | Frequency(f) | fx |
|----------------|------------------|------------------|------|
| 0-50 | 25 | 15 | 375 |
| 50-100 | 75 | 20 | 1500 |
| 100-150 | 125 | 35 | 4375 |
| 150-200 | 175 | 20 | 3500 |
| 200-250 | 225 | 10 | 2250 |

$$\Sigma f = 100 \quad \Sigma fx = 12000$$

$$\therefore \text{Arithmetic mean} = \frac{\Sigma fx}{\Sigma f}$$

$$= \frac{12000}{100}$$

$$= 120$$

$$\therefore \text{Arithmetic mean} = 120$$

Questions:

1. Find the arithmetic mean of the following frequency distribution.

| | | | | | | | | |
|-----------------|------|-------|-------|-------|-------|-------|-------|-------|
| Marks obtained | 0-10 | 10-20 | 20-30 | 30-40 | 40-50 | 50-60 | 60-70 | 70-80 |
| No. of students | 3 | 8 | 12 | 14 | 10 | 6 | 5 | 2 |

2. Find the arithmetic mean of the following frequency distribution.

| | | | | | | | |
|----------------|------|-------|-------|-------|--------|---------|---------|
| Class interval | 0-20 | 20-40 | 40-60 | 60-80 | 80-100 | 100-120 | 120-140 |
| frequency | 12 | 18 | 15 | 25 | 26 | 15 | 9 |

3. Find the arithmetic mean of the following frequency distribution.

| | | | | | | | |
|----------------|---------|---------|---------|---------|---------|---------|---------|
| Class interval | 130-135 | 135-140 | 140-145 | 145-150 | 150-155 | 155-160 | 160-165 |
| frequency | 7 | 16 | 30 | 26 | 18 | 13 | 5 |

4. Find the arithmetic mean of the following frequency distribution.

| | | | | | | | | |
|----------------|---------|---------|---------|---------|---------|---------|---------|---------|
| Class interval | 300-309 | 310-319 | 320-329 | 330-339 | 340-349 | 350-359 | 360-369 | 370-379 |
| Frequency | 8 | 21 | 26 | 41 | 49 | 28 | 19 | 8 |

WORKSHEET-5

ii) The arithmetic mean of the following frequency is 25. Find the value of P.

| | | | | | |
|----------------|------|-------|-------|-------|-------|
| Class interval | 0-10 | 10-20 | 20-30 | 30-40 | 40-50 |
| Frequency | 5 | 8 | 15 | P | 6 |

Solution:

| Class interval | Mid point(x) | Frequency(f) | fx |
|----------------|------------------|------------------|------|
| 0-10 | 5 | 5 | 25 |
| 10-20 | 15 | 8 | 120 |
| 20-30 | 25 | 15 | 375 |
| 30-40 | 35 | P | 35P |
| 40-50 | 45 | 6 | 270 |

$$\Sigma f = 34 + P \quad \Sigma fx = 790 + 35P$$

$$\therefore \text{Arithmetic mean} = \frac{\Sigma fx}{\Sigma f}$$

$$\Rightarrow 25 = \frac{790 + 35P}{34 + P}$$

$$\Rightarrow 25(34 + P) = 790 + 35P$$

$$\Rightarrow 850 + 25P = 790 + 35P$$

$$\Rightarrow 850 - 790 = 35P - 25P$$

$$\Rightarrow 60 = 10P$$

$$\Rightarrow P = \frac{60}{10}$$

$$\Rightarrow P = 6$$

Questions:

1. The arithmetic mean of the following frequency is 28. Find the value of f_1

| | | | | | | |
|-----------------|------|-------|-------|-------|-------|-------|
| Marks | 0-10 | 10-20 | 20-30 | 30-40 | 40-50 | 50-60 |
| No. of students | 12 | 18 | 27 | f_1 | 17 | 6 |

2. The arithmetic mean of the following frequency is 27. Find the value of p .

| | | | | | |
|-----------------|------|-------|-------|-------|-------|
| Marks | 0-10 | 10-20 | 20-30 | 30-40 | 40-50 |
| No. of students | 2 | 4 | p | 7 | 3 |