

## SURDS

Explain rational number, irrational number.

Explain surds.

eg.  $\sqrt{2}, \sqrt{3}, \sqrt{5}, \sqrt{7}, 2\sqrt{2}, 2\sqrt{3}, 3\sqrt{5}, \dots$  etc

Conversion into simplest form

eg.  $\sqrt{8} = \sqrt{2 \times 2 \times 2} = 2\sqrt{2}$

i.  $\sqrt{8}$

ii.  $\sqrt{32}$

iii.  $\sqrt{27}$

iv.  $\sqrt{12}$

v.  $\sqrt{20}$

vi.  $\sqrt{24}$

vii.  $\sqrt{75}$

viii.  $\sqrt{48}$

ix.  $\sqrt{28}$

x.  $\sqrt{44}$

### Addition

1.  $2\sqrt{3} + \sqrt{3} = 3\sqrt{3}$

2.  $5\sqrt{7} + \sqrt{7} = 6\sqrt{7}$

Add the following:

i.  $2\sqrt{3} + 5\sqrt{3}$

ii.  $3\sqrt{2} + 4\sqrt{2}$

iii.  $\sqrt{8} + \sqrt{2}$

iv.  $4\sqrt{3} + \sqrt{75}$

v.  $2\sqrt{3} + \sqrt{3} + 5\sqrt{3}$

vi.  $4\sqrt{3} + 3\sqrt{2} + \sqrt{75}$

### Subtraction

1.  $4\sqrt{2} - 3\sqrt{2} = \sqrt{2}$

2.  $7\sqrt{3} - 4\sqrt{3} = 3\sqrt{3}$

Subtract the following:

i.  $4\sqrt{2} - \sqrt{2}$

ii.  $4\sqrt{3} - 2\sqrt{3}$

iii.  $3\sqrt{6} - \sqrt{6}$

iv.  $5\sqrt{7} - 2\sqrt{7}$

v.  $4\sqrt{5} - \sqrt{20}$

vi.  $4\sqrt{3} - \sqrt{3} - \sqrt{12}$

## Multiplication

$$1. \sqrt{2} \times \sqrt{3} = \sqrt{6}$$

$$2. 5\sqrt{2} \times 2\sqrt{3} = 10\sqrt{6}$$

Multiply

$$\text{i. } \sqrt{5} \times \sqrt{3}$$

$$\text{ii. } \sqrt{2} \times \sqrt{5}$$

$$\text{iii. } \sqrt{2} \times \sqrt{7}$$

$$\text{iv. } \sqrt{2} \times \sqrt{3}$$

$$\text{v. } \sqrt{3} \times \sqrt{3}$$

$$\text{vi. } \sqrt{6} \times \sqrt{3}$$

$$\text{vii. } \sqrt{2} \times \sqrt{3}$$

$$\text{viii. } \sqrt{10} \times \sqrt{2}$$

$$\text{ix. } 5\sqrt{2} \times 2\sqrt{3}$$

$$\text{x. } \sqrt{3} \times 2\sqrt{8}$$

$$\text{xi. } 3\sqrt{2} \times 2\sqrt{5}$$

$$\text{xii. } 2\sqrt{2} \times \sqrt{3}$$

$$\text{xiii. } 6\sqrt{2} \times 2\sqrt{3}$$

$$\text{xiv. } 5\sqrt{5} \times 2\sqrt{3}$$

$$\text{xv. } \sqrt{7} \times 2\sqrt{3}$$

$$\text{xiv. } \sqrt{2} \times 2\sqrt{5}$$

## Simplify:

$$\text{i. } 2\sqrt{3} + \sqrt{12}$$

$$\text{ii. } 2\sqrt{2} + \sqrt{50}$$

$$\text{iii. } 5\sqrt{24} + 2\sqrt{6}$$

$$\text{iv. } 3\sqrt{8} - \sqrt{32}$$

$$\text{v. } 3\sqrt{8} - 2\sqrt{12} + \sqrt{20}$$

$$\text{vi. } 3\sqrt{18} - 2\sqrt{27} + \sqrt{45}$$

$$\text{vii. } 5\sqrt{3} - 2\sqrt{12} - \sqrt{32} + \sqrt{50}$$

$$\text{viii. } 3\sqrt{6} - 2\sqrt{24} - \sqrt{54} + \sqrt{150}$$

$$\text{eg. } 2\sqrt{3} + \sqrt{12} = 2\sqrt{3} + \sqrt{2 \times 2 \times 3}$$

$$= 2\sqrt{3} + 2\sqrt{3}$$

$$= 4\sqrt{3}$$

## RATIONALIZATION OF SURDS:

Explain rationalization of surds:

eg. The rationalization of  $2 + \sqrt{3}$  is

$$\begin{aligned}(2 + \sqrt{3})(2 - \sqrt{3}) &= (2)^2 - (\sqrt{3})^2 \\ &= 4 - 3 \\ &= 1\end{aligned}$$

Rationalize the following:

i.  $2 + \sqrt{3}$

ii.  $3 + \sqrt{7}$

iii.  $3 + \sqrt{5}$

iv.  $5 + \sqrt{21}$

v.  $\sqrt{6} + \sqrt{3}$

vi.  $\sqrt{3} + \sqrt{2}$

vii.  $\sqrt{2} + 1$

viii.  $\sqrt{6} + \sqrt{5}$

ix.  $2\sqrt{2} + \sqrt{3}$

x.  $2\sqrt{3} + \sqrt{5}$

xi.  $2\sqrt{3} + \sqrt{10}$

xii.  $\sqrt{3} - \sqrt{2}$

xiii.  $\sqrt{75} - \sqrt{50}$

xiv.  $2\sqrt{7} - 5$

xv.  $4 - 2\sqrt{3}$

xvi.  $5\sqrt{3} - 3\sqrt{6}$

**Simplification:** Eg.  $\frac{\sqrt{5}}{\sqrt{3}-\sqrt{2}}$

$$= \frac{\sqrt{5}}{\sqrt{3}-\sqrt{2}} \times \frac{(\sqrt{3}+\sqrt{2})}{(\sqrt{3}+\sqrt{2})}$$

$$= \frac{\sqrt{5} (\sqrt{3}+\sqrt{2})}{(\sqrt{3}-\sqrt{2})(\sqrt{3}+\sqrt{2})}$$

$$= \frac{\sqrt{15}+\sqrt{10}}{(\sqrt{3})^2-(\sqrt{2})^2}$$

$$= \frac{\sqrt{15}+\sqrt{10}}{3-2}$$

$$= \sqrt{15} + \sqrt{10}$$

Simplify:

i.  $\frac{3}{\sqrt{3}-\sqrt{2}}$

ii.  $\frac{3}{\sqrt{6}-\sqrt{3}}$

iii.  $\frac{3\sqrt{3}}{\sqrt{5}-\sqrt{2}}$

iv.  $\frac{2\sqrt{2}}{\sqrt{5}+\sqrt{3}}$

v.  $\frac{2}{\sqrt{7}-\sqrt{3}}$

vi.  $\frac{\sqrt{7}+\sqrt{3}}{5+\sqrt{21}}$

vii.  $\frac{\sqrt{5}}{\sqrt{3}-\sqrt{2}} - \frac{3\sqrt{3}}{\sqrt{5}-\sqrt{2}} - \frac{2\sqrt{2}}{\sqrt{5}+\sqrt{3}}$

viii.  $\frac{3\sqrt{7}}{\sqrt{5}+\sqrt{2}} - \frac{5\sqrt{5}}{\sqrt{7}+\sqrt{2}} + \frac{2\sqrt{2}}{\sqrt{7}+\sqrt{5}}$

ix.  $\frac{3\sqrt{2}}{\sqrt{6}-\sqrt{3}} - \frac{4\sqrt{3}}{\sqrt{6}-\sqrt{2}} + \frac{2\sqrt{3}}{\sqrt{6}+\sqrt{2}}$

x.  $\frac{3\sqrt{7}}{\sqrt{5}+\sqrt{2}} - \frac{5\sqrt{5}}{\sqrt{2}+\sqrt{7}} + \frac{2\sqrt{2}}{\sqrt{7}+\sqrt{5}}$  xi.  $\frac{\sqrt{2}}{\sqrt{3}} \left( \frac{2+\sqrt{3}}{\sqrt{3}+1} \right) - \frac{\sqrt{2}}{\sqrt{3}} \left( \frac{2-\sqrt{3}}{\sqrt{3}-1} \right)$

Some extra questions

1. If  $x = \sqrt{\frac{\sqrt{5}+1}{\sqrt{5}-1}}$ , prove that  $x^2 - x = 1$

2. If  $x = \frac{\sqrt{3}+\sqrt{2}}{\sqrt{3}-\sqrt{2}}$  &  $xy = 1$ , then find the value of  $7x^2 - 5xy + 7x^2$ .